

# Comparing the adjoint- and ensemble-based approaches to observation impact on short-range forecasts

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## Outline



Introduction

Recap of FSOI Basics

Preliminary Results

Closing Remarks

# FSOI at GMAO: from Adjoint- to Ensemble-based?



#### Evolution of Forecast Sensitivity and Observation Impact (FSOI) at GMAO:

- GMAO has been calculating FSOI in its Forward Processing (FP) system for several years.
- FP has evolved from 3dVar to Hybrid-3dVar to what is presently Hybrid-4dEnVar.
- Our strategy follows the Langland & Baker (2004) approach and relies on the availability of an adjoint model.
- Along the years the GMAO forward model has gone from FV to FV<sup>3</sup>; accordingly, the adjoint model has gone from AD-FV to AD-FV<sup>3</sup>.
- Linearized physics, and corresponding adjoint, has evolved from simple diffusion and vertical drag to more elaborate accountability of convection (Holdaway, Errico, Gelaro & Kim).

#### Ensemble DA opens the door to bypass the Adjoint Model:

- In a dual-analysis system (Var & Ens) the possibility exists to base FSOI fully on the ensemble - this has its caveats (see what follows).
- Alternatively:
- Method I The AD-Var-analysis can be adapted to make use of an ensemble forecast to implicitly estimate forecast sensitivities;
- Method II Or, similarly, but not identically, the ensemble might be used to explicitly estimate forecast sensitivities required by the AD-Var-analysis.

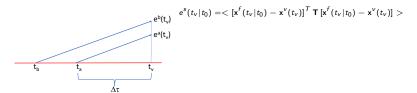
This presentation provides insights from preliminary evaluation of these possibilities.



#### Error reduction measure and FSOI



#### Forecast error:



The impact of observations is typically evaluated by studying how the error measure above changes as a consequence of assimilating observations. Whether based on  $\frac{\text{adjoint}}{\text{or ensemble}}$  techniques, these methods require evaluation of expressions of the form:

$$\delta e \, pprox < \mathbf{d}^T \mathbf{K}^T \mathbf{g}_0 >$$

with d and K being the background residual vector and the analysis gain matrix, and g amounting to a forecast sensitivity vector whose approximation leads to all kinds of formula.

	AD-Solver ( <b>K</b> ' )	Forecast Sensitivity $(\mathbf{g}_0)$	This Talk
VA-FSOI	Var	ADM	done
EE-FSOI	En	En	done
VE-FSOI	Var	En	done
EA-FSOI	En	ADM	_





VA-FSOI vs EE-FSOI in a Dual-Analysis Hybrid System

## Adjoint- and Ensemble-based FSOI



#### Variational-Adjoint-FSOI (VA-FSOI)

Second-order Approximation (Trapezoidal rule; Langland & Baker 2004; Tellus):

$$\mathbf{g}_{0}^{A} \equiv \frac{1}{2}(\mathbf{M}_{a}^{T}\mathbf{T}\mathbf{e}^{a} + \mathbf{M}_{b}^{T}\mathbf{T}\mathbf{e}^{b}).$$

And in a system such as GSI, the calculation of  $\delta e$  can be done as in:

$$\delta e \approx < \mathbf{d}^T \mathbf{R}^{-1} \mathbf{H} \tilde{\mathbf{g}} >,$$

where  $\tilde{\mathbf{g}}$  is derived from the GSI-hybrid solver as in (double-CG or Bi-CG):

$$(B + BH^TR^{-1}HB)z = Bg_0^A$$
  
 $\tilde{g} = Bz$ 

for 
$$\mathbf{B} = \beta_c \mathbf{B}_c + \beta_e \mathbf{B}_e$$
.

#### Ensemble-Ensemble-FSOI (EE-FSOI)

In Ensemble systems, the gradient is defined with respect to the ensemble mean:

$$\mathbf{g}_0^E \equiv \frac{1}{2} \mathbf{X}_a^{fT} \mathbf{T} (\bar{\mathbf{e}}^a + \bar{\mathbf{e}}^b),$$

where  $\mathbf{X}_{a}^{f} \equiv \mathbf{X}^{f}(t_{v}|t_{a})$  is a matrix created from the ensemble perturbation of forecasts issued from  $t_{a}$  and valid at  $t_{v}$ , and the over-bar represents ensemble average.

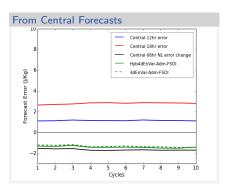
And in a system such as the EnSRF, calculation of  $\delta e$  amount to:

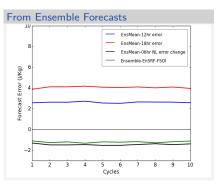
$$\delta e pprox rac{1}{2} < \mathbf{d}^\mathsf{T} \mathbf{R}^{-1} \mathbf{H} \left( \mathbf{L} ullet \mathbf{X}^a \mathbf{X}^{fT} \right) \mathbf{T} (\bar{\mathbf{e}}^a + \bar{\mathbf{e}}^b) >,$$

where  $\mathbf{X}_a \equiv \mathbf{X}_a(t_a)$  is a matrix formed from ensemble analysis perturbations (Kalnay et~al., 2012, Tellus; Ota et~al., 2013, Tellus). An argument has been made to have  $\mathbf{L}$  above as an advected form of the  $\mathbf{L}$  used in the forward ensemble analysis.

## VA-FSOI vs EE-FSOI







- ▶ Error reductions are similar between central and ensemble forecasts, thought latter is slightly smaller in absolute value for 12-hour forecasts.
- ▶ Left: compares FSOI when backward Var changed from Hyb-4dEnVar to 4dEnVar.
- ► Right: presents EE-FSOI.

## VA-FSOI vs EE-FSOI

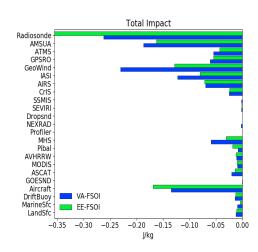
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#### Total Impact

- ➤ To render a fair comparison, we calculate Adjoint-based impacts for a changed Adjoint analysis integration where the climatological term is shut off, thus converting the backward run into a 4dEnVar instead of its default (FP-like) Hybrid-4dEnVar.
- At first glance, impact rankings are similar.
- Closer examination reveals considerable differences (e.g., radiosondes and satellite winds).
- Differences are also non-negligible for MW and IR satellite radiances (AMSU-A, ATMS, IASI).

#### Overall this comparison reflects that:

- Ensemble mean forecasts are unrelated to the central forecast.
- But more importantly, the ensemble analysis handles observations largely differently to how the hybrid analysis does.



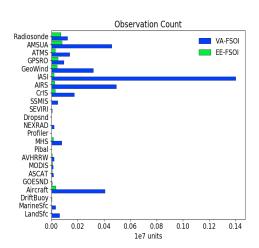
## VA-FSOI vs EE-FSOI

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#### Observation Counts

- The difference in treatment of observations between ensemble and central analyses is evidenced in the observation count.
- The GSI and EnSRF solvers have considerably different convergence criteria.
- Even with the ideal DFS-based criterium (chosen here), the EnSRF ignores a very large percentage of the observations.

All-in-all we don't think observation impacts derived from the En-SRF solver represent well how the deterministic (central) analysis system uses observations.





VA-FSOI vs VE-FSOI in a Dual-Analysis Hybrid System

## VA-FSOL vs VF-FSOL



## Variational-Ensemble-FSOI (VE-FSOI) Method I

As in Buehner et al. (2018, MWR), in a EnVar, such that  $B=B_{\rm e}$ , the ensemble background covariance allows for the following to be written

$$\mathbf{B}_{e}\mathbf{g}_{0}^{A} = \mathbf{L} \bullet \mathbf{X}_{b}(\mathbf{X}_{b})^{T}\mathbf{g}_{0}^{A}$$

$$\approx \mathbf{L} \bullet \mathbf{X}_{b}\mathbf{X}_{a}^{T}\mathbf{M}^{T}(t_{a}, t_{b})\mathbf{g}_{0}^{A}$$

We can replace  $\mathbf{g}_0^A$  with  $\mathbf{g}_0^E$  (using central forecast errors) in the RHS to get

$$\begin{aligned} \mathbf{B}_{e}\mathbf{g}_{0}^{A} & \approx & \mathbf{B}_{e}\mathbf{g}_{0}^{E} \\ & \approx & \frac{1}{2}\mathbf{L} \bullet \mathbf{X}_{b}\mathbf{X}_{a}^{T}\mathbf{M}^{T}(t_{a},t_{b})\mathbf{X}_{a}^{fT}\mathbf{T}(\mathbf{e}^{a}+\mathbf{e}^{b}) \\ & = & \frac{1}{2}\mathbf{L} \bullet \mathbf{X}_{b}\mathbf{X}_{b}^{fT}\mathbf{T}(\mathbf{e}^{a}+\mathbf{e}^{b}) \end{aligned}$$

which amounts to a simple change to the RHS of the minimization problem solved for calculation of observation impacts in the Var system. Note:  $\mathbf{e}^{a}(\mathbf{e}^{b})$  replaces  $\mathbf{\bar{e}}^{a}(\mathbf{\bar{e}}^{b})$ 

# Variational-Ensemble-FSOI (VE-FSOI) Method II

Alternatively, we can try to use the approach of Ancell & Hakim (2007; MWR) to estimate forecast sensitivities using an ensemble of forecasts.

In this case, the forecast sensitivity is estimated as in:  $\begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}$ 

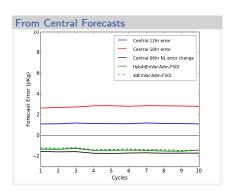
$$\frac{\partial f}{\partial \mathbf{x}} = \mathbf{D}^{-1} \begin{bmatrix} \frac{\delta \mathbf{x}_1 \delta \mathbf{e}_1'}{\delta \mathbf{x}_2 \delta \mathbf{e}_2'} \\ \vdots \\ \delta \mathbf{x}_n \delta \mathbf{e}_n^T \end{bmatrix}$$

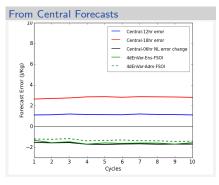
where  $\mathbf{D} = diag(||\delta \mathbf{x}_1||^2, ||\delta \mathbf{x}_2||^2, \cdots, ||\delta \mathbf{x}_n||^2)$ ,  $dim(\mathbf{x}_i) = dim(\mathbf{e}_i) = M \times 1$ , and n is the state-space dimension.

This presentation will not present results for Method II.

## VA-FSOI vs VE-FSOI Method I







- Lack of advection of localization scales in the RHS of the Var impact expression motivates following Buehner *et al.* (2018; MWR) and evaluating 12-hr instead of 24-hr FSOI.
- ▶ Left: compares FSOI when backward Var changed from Hyb-4dEnVar to 4dEnVar.
- ▶ Right: compares VA-FSOI with VE-FSOI Method I.

**Remark**: 32-member ensemble perturbations seem rather reasonable replacement for ADM for 12-hr sensitivity calculation in 4dEnVar context.

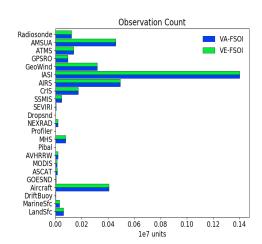


#### VA-FSOI vs VE-FSOI Method I

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#### Observation Counts

- The two approaches treat the observations in exactly the same way, and fully consistent with how the forward (Hyb-4dEnVar) solver treats them.
- Replacing the Adjoint Model with Ensemble perturbations to estimate forecast sensitivities leaves the analysis solver untouched wrt each other.
- The figure on the right shows observation counts between the VA-FSOI and VE-FSOI Method I techniques, for backward integrations of 4dEnVar, covering a 10-day period.

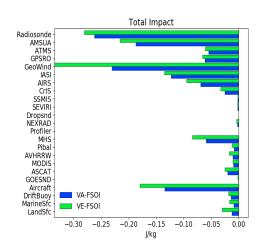


## VA-FSOI vs VE-FSOI Method I

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#### Total Impact

- Overall, impacts don't seem to change much and are largely comparable when ADM is replaced with Ensemble perturbations.
- Closer look reveals satellite winds (GeoWind), MW sensors (MHS, AMSU-A), aircrafts and near surface observations to have larger impact when Ens-Perts are used compared to when ADM is used to estimate forecast sensitivity.
- The above seems to be consistent with the fact that the simply parameterized adjoint physics is expected to mis-represent water and near surface fields as compared to the full GCM.



## Closing Remarks



- More importantly, though the observation operators in the hybrid GSI and EnSRF are shared, GSI and EnSRF treat observations rather differently.
- ▶ In a dual hybrid DA system, when a (low resolution) ensemble analysis filter is used to provide flow dependence to a (high resolution) hybrid analysis, certain configurations of the ensemble filter might discourage assessing observation impact using the EE-FSOI based on the EnDA part of system.
- ► The comment above applies particularly to GSI-EnSRF-based systems.
- As in Buehner *et al.*, we have shown that it is possible to enable the Var system to derive observation impacts with forecast sensitivities calculated from the ensemble thus avoiding the adjoint model.

